

Delphine's handy dandy units and formula sheet

**DIFFUSION**

Important Quantities and their units:

$x$	position	[cm]
$t$	time	[sec]
$c(x,t)$	concentration	$[\frac{\text{mole}}{\text{cm}^3}]$
$f$	diffusive flux	$[\frac{\text{mole}}{\text{sec} \cdot \text{cm}^2}]$
$D$	diffusivity	$[\frac{\text{cm}^2}{\text{sec}}]$
$k$	partitioning coefficient	[unitless]
$P$	permeability	$[\frac{\text{cm}}{\text{sec}}]$
$\tau_{SS}$	steady state time constant	[sec]
$\tau_{EQ}$	equilibrium time constant	[sec]

General Equations:

$$f(x,t) = -D \frac{\partial}{\partial x} (c(x,t)) \quad \text{Fick's First Law}$$

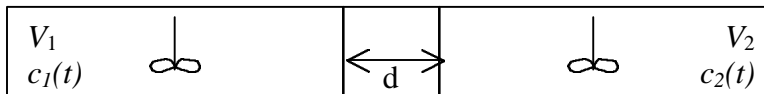
$$-\frac{\partial}{\partial x} f(x,t) = \frac{\partial}{\partial t} (c(x,t)) \quad \text{Continuity Equation}$$

combine to get:

$$\frac{\partial}{\partial t} (c(x,t)) = D \frac{\partial^2}{\partial x^2} (c(x,t)) \quad \text{Diffusion Equation}$$

if you have a partition coefficient,  $k$ , then stick  $k$  with  $D$  in the above equations.

2-Compartment Model:



$$P = \frac{kD}{d} \quad \text{Membrane Permeability}$$

$$t_{SS} = \frac{d^2}{P^2 D} \quad \text{Steady State Time Constant}$$

$$t_{EQ} = \frac{1}{AP \left( \frac{1}{V_1} + \frac{1}{V_2} \right)} \quad \text{Equilibrium Time Constant}$$

if  $t_{SS} \ll t_{EQ}$  (thin membrane) and at steady state then:

$$f = P(c^1(t) - c^2(t)) \quad \text{Fick's Law for membranes}$$